

# Indecision Modeling

Duncan C McElfresh<sup>1</sup>, Lok Chan<sup>2</sup>, Kenzie Doyle<sup>3</sup>, Walter Sinnott-Armstrong<sup>2</sup>, Vincent Conitzer<sup>2</sup>, Jana Schaich Borg<sup>2</sup>, John P Dickerson<sup>1</sup>

1: University of Maryland, College Park  
2: Duke University  
3: University of Oregon

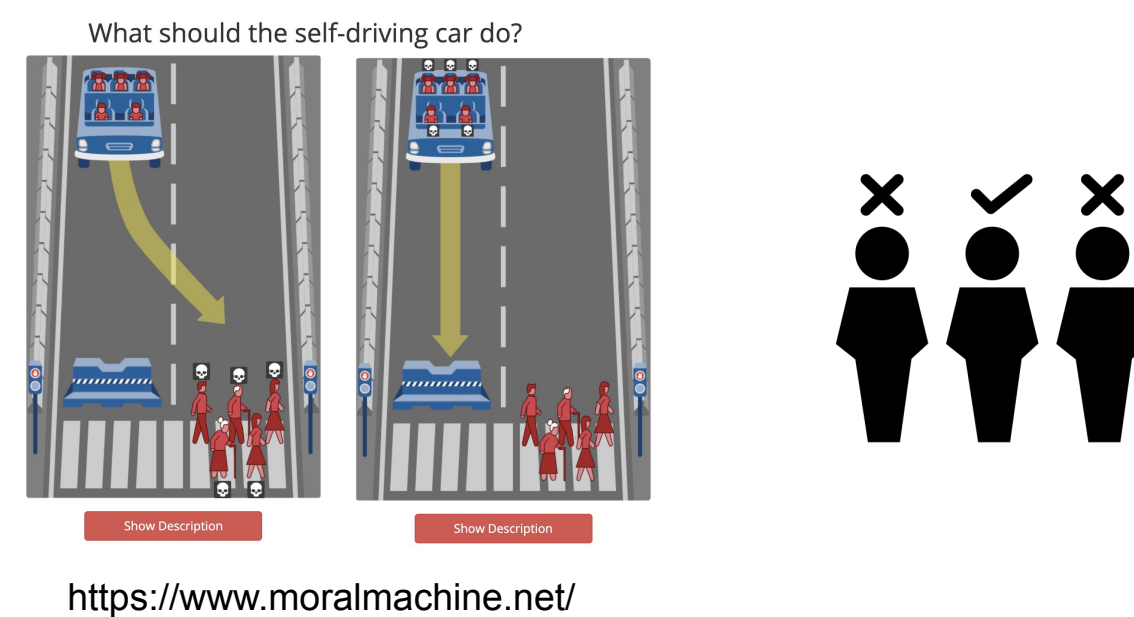
Preprint: <https://arxiv.org/abs/2012.08485>

## Motivation: Preference Modeling & AI

Many AI systems used to **make** or **contribute to important decisions** are guided by **mathematical models of stakeholder preferences**.

**Our main motivation:** Preference aggregation for policy design  
Stakeholder preferences are *learned* and *aggregated* to make important decisions. The literature has considered applications of...

- Self-driving cars [Noothigattu et al., 2018]
- Kidney exchange [Freedman et al., 2020]

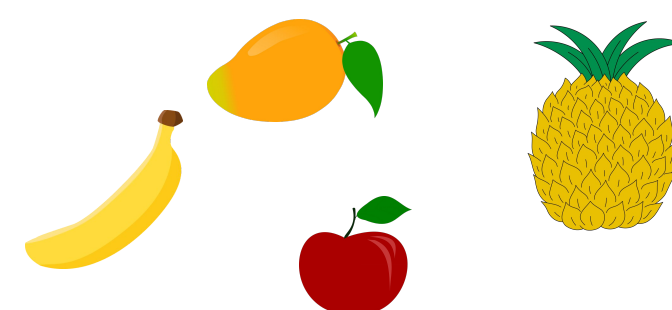


## Background: Preference Modeling & Indecision

### Decision-maker (“Agent”)



### Alternatives



**Assumption:** Agent decisions are consistent with a preference relation:  
for each pair of alternatives (i, j) either...

- $i > j$  “i is more-preferred than j”, or
- $i < j$  “i is less-preferred than j”, or
- $i \approx j$  “neither  $i > j$  nor  $i < j$ ”

**Assumption:** Preferences are...

- Complete (defined for all (i, j) pairs)
- Transitive:
  - $i > j$  and  $j > k$  imply  $i > k$
  - $i \approx j$  and  $j \approx k$  imply  $i \approx k$

There exists a *utility function* representation for preferences, s.t.

- $u(i) > u(j) \Leftrightarrow i > j$
- $u(i) = u(j) \Leftrightarrow i \approx j$

However, agents may sometimes be *indecisive*...

What if i and j are **not comparable**? [Pini’11]

What if the agent doesn’t want to “**play God**” [Gangemi’13]

## Our Contributions

**We test & reject the assumption:**

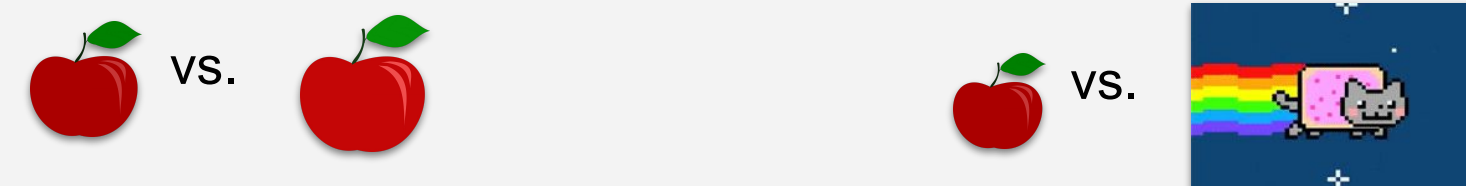
“indecision”  $\Leftrightarrow$  “alternatives are equally preferred”

- (1) **We explore possible causes of indecision, and develop a modeling framework for hypothesis testing.**

## Causes for Indecision

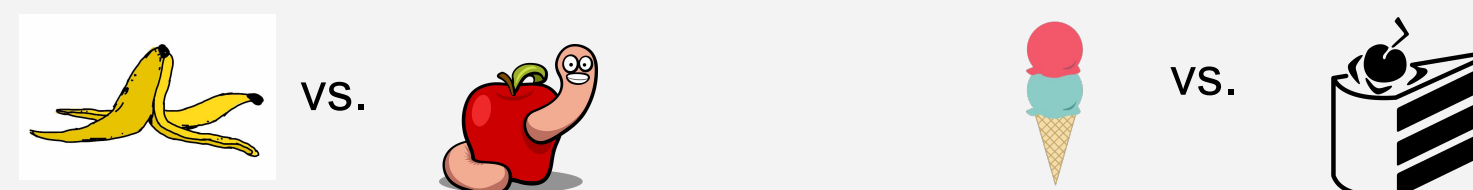
### Difference-Based Indecision

...when the *perceived difference* between X and Y is too small (or too large) to arrive at a strict preference.



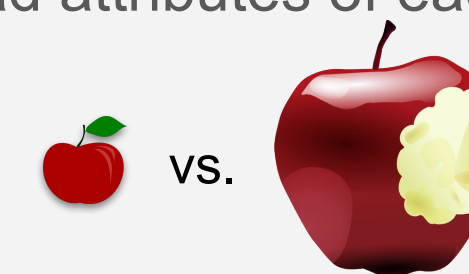
### Desirability-Based Indecision

...when both X and Y are “too bad” (or “too good”). [Zakay’84] [Luce’98]



### Conflict-based Indecision

...when there are both good and bad attributes of each alternative. [Tversky’92]



## Indecision Modeling Framework

### Example

#### Desirability-Based Indecision



... indecisive when both items are *below* utility threshold  $\lambda$

### (A) Response function

$$R(i, j) \equiv \begin{cases} > & \text{if } u(i) \geq \max\{u(j), \lambda\} \\ < & \text{if } u(j) \geq \max\{u(i), \lambda\} \\ \approx & \text{if } \lambda \geq \max\{u(i), u(j)\} \end{cases}$$



### (B) Equivalent “score-based” response function

$$S_{>}(i, j) \equiv u(i) \\ S_{<}(i, j) \equiv u(j) \\ S_{\approx}(i, j) \equiv \lambda \\ R(i, j) = \arg \max_{r \in \{<, >, \approx\}} S_r(i, j)$$

## Study 1: indecision $\neq$ indifference

### Hypothetical Decision Scenario:

Participants choose to give a donor kidney to one of two patients.

Participants “**vote**” for a patient...

- some are *forced to choose*
- some can be indecisive ( $\approx$ )

Without ( $\approx$ )	Votes	
	A > B	A < B
With ( $\approx$ )	A > B	A < B
		A $\approx$ B

Choose A		Flip a coin	Choose B	
Patient A			Patient B	
3	drinks per day prediagnosis		4	drinks per day prediagnosis
47	years old		68	years old
2	child dependent(s)		2	child dependent(s)

Example question used in our surveys.

We **reject** ( $p < 0.01$ ) the hypothesis:

*Indecisive voters prefer both alternatives equally.*

For our participants, “**indecision**” does not mean  
“**both alternatives are equally preferred**”

## Questions for Future Work

**Q:** How do we *aggregate* indecisive stakeholders’ preferences, when indecision has several meanings?

Are traditional social choice methods appropriate?

**Q:** What if we *ask* people why they are indecisive?

Will their responses match any of our models?

**Q:** How do we elicit different causes of indecision without a communication bottleneck?

### References

- Freedman, Rachel, et al. "Adapting a kidney exchange algorithm to align with human values." (AIJ, 2020)
- Noothigattu, Ritesh, et al. "A voting-based system for ethical decision making." (AAAI’18)
- Pini et al’ “Incompleteness and incomparability in preference aggregation: Complexity results” (AIJ, 2011)
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